



**12<sup>th</sup> Meeting of the International Group on Research Reactors (IGORR 12)**  
**Beijing, China, October 28-30, 2009**

***Fundamental Research on Molten Salt Reactors***

**Zhang Dalin, Qiu Suizheng, Su Guanghui**

*Xi'an Jiaotong University, Xi'an, 710049, China*



## **Outline**



### **Introduction**



### **Actual work:**

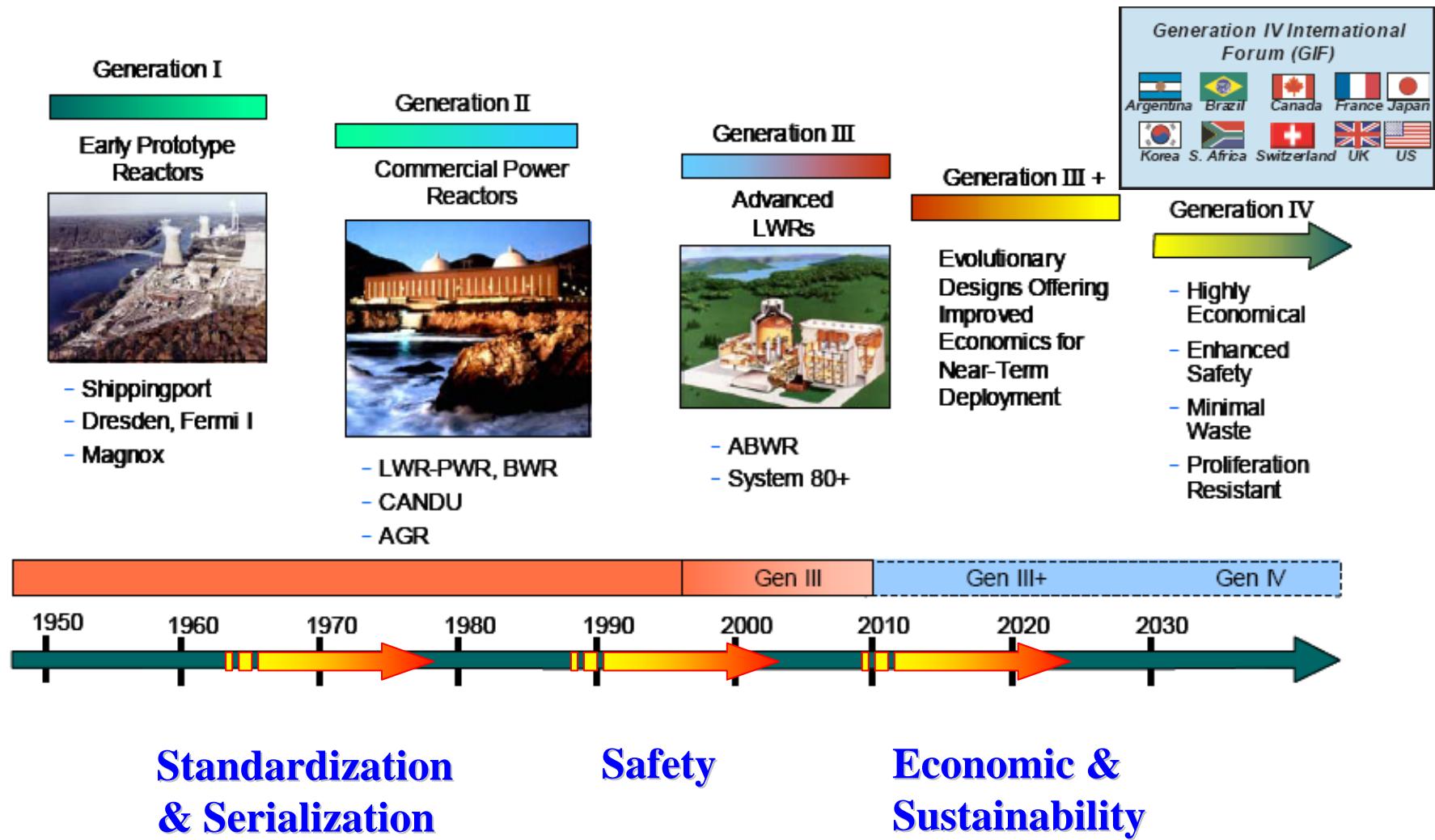
- Thermophysical properties
- Neutronics
- Thermohydraulics
- Safety



### **Concluding remarks**



### ➤ Overview of the Generations of Nuclear Energy Systems





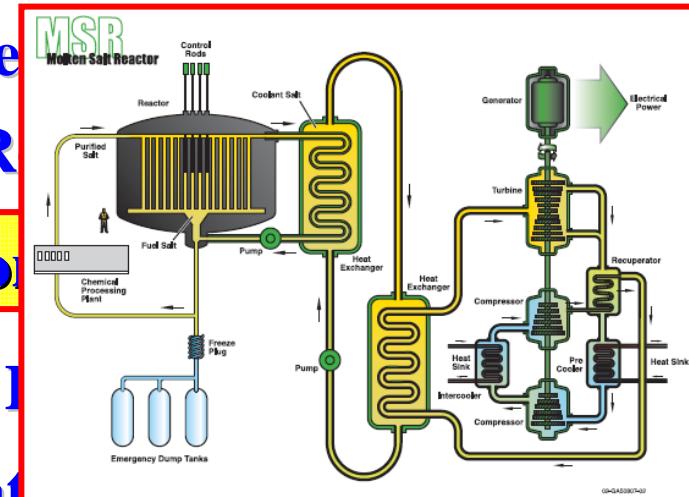
### ➤ Goals for Generation IV Nuclear Energy Systems and Selections

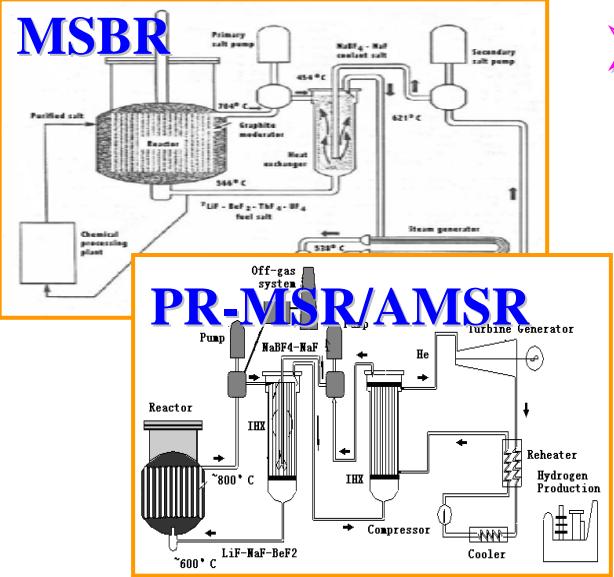
Goals {

- Sustainability
- Economics
- Safety and Reliability
- Proliferation Resistance and Physical Protection

Selections {

- GFR: Gas-Cooled Fast Reactor
- LFR: Lead-Cooled Fast Reactor
- MSR: Molten Salt Reactor**
- SFR: Sodium-Cooled fast Reactor
- SCWR: Supercritical-Water Reactor
- VHTR: Very-High-Temperature Reactor





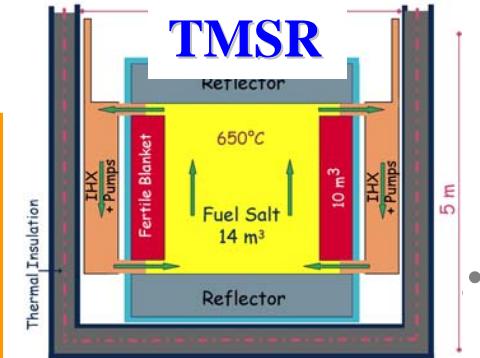
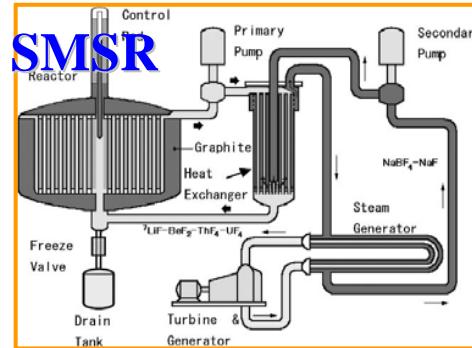
ORNL: **MSRE**,  
8MW, 13000  
hours.

1960s

1954

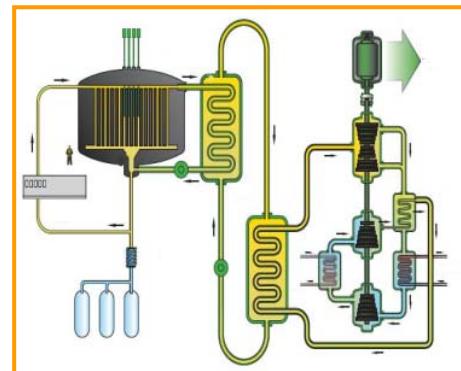
ORNL: **ARE**, 2.5MW,  
for the nuclear engine  
of the military jet  
aircraft.

## ➤ Introduction of MSR (1)



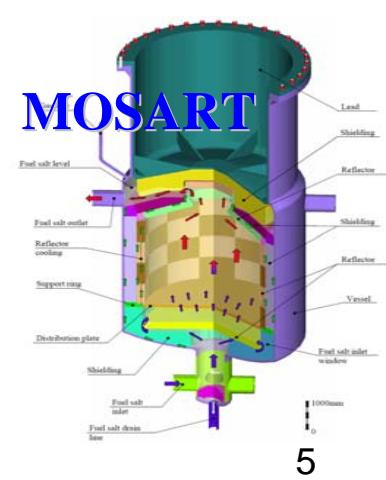
now

SMSR  
MOSART  
TMSR



1979

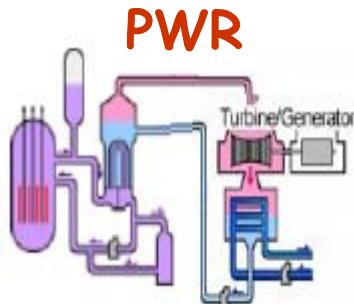
GIF proposed six  
of generation IV r  
SCWR, VHTR, M  
LFR, GFR.





## ➤ Introduction of MSR (2)

- Liquid fuel
- Pressure < 0.5MPa
- Outflow Temperature >700°C
- Brayton cycle



- Solid fuel
- Pressure: 15MPa
- Outflow T: 330°C
- Rankine cycle

### Advantages:

- Inherent safety feature
- Excellent neutron economy
- High thermal efficiency 45-50%
- Continuous or in-batch reprocessing
- Non-proliferation

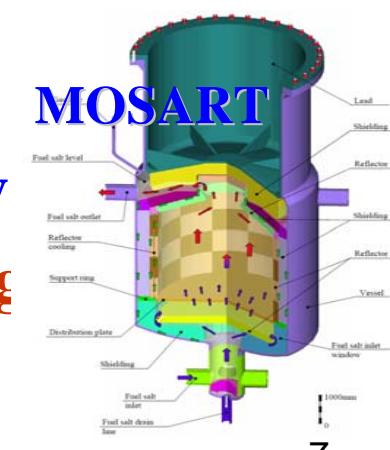
### Technology bases:

- Prototype reactors: ARE and MSRE
- Technologies for high temperature reactors:  
Brayton cycles  
Compact heat exchanges  
C-C composites



## ➤ **Technology Gaps for MSRs**

- Molten salt chemistry and control
- Solubility of minor actinides and lanthanides in the fuel
- Compatibility of irradiated molten salt fuel with structural materials
- Salt processing, separation, and reprocessing technology
- Fuel development, new cross section data
- Corrosion and embrittlement studies
- Development of tritium control technology
- Graphite sealing technology and graphite stability
- Detailed conceptual design studies to develop design specifications
- .....

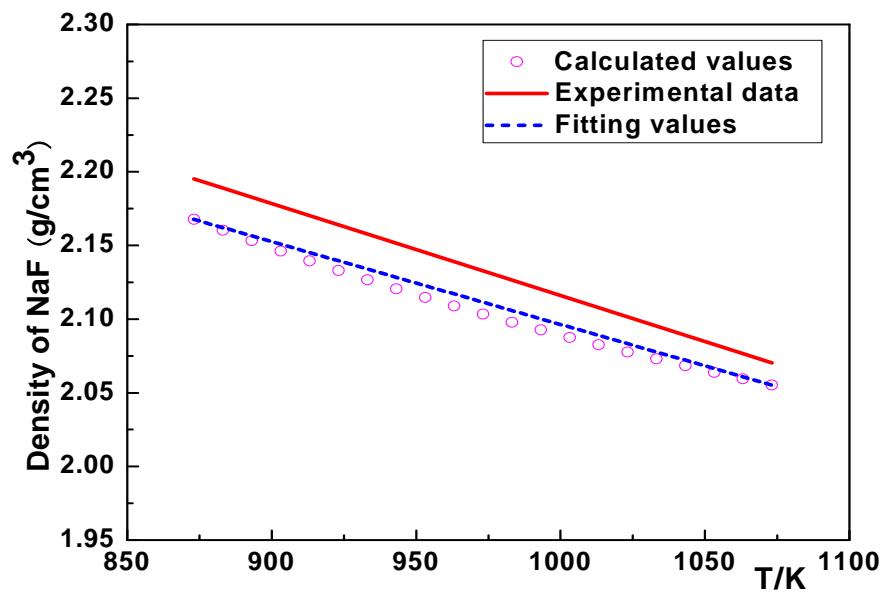
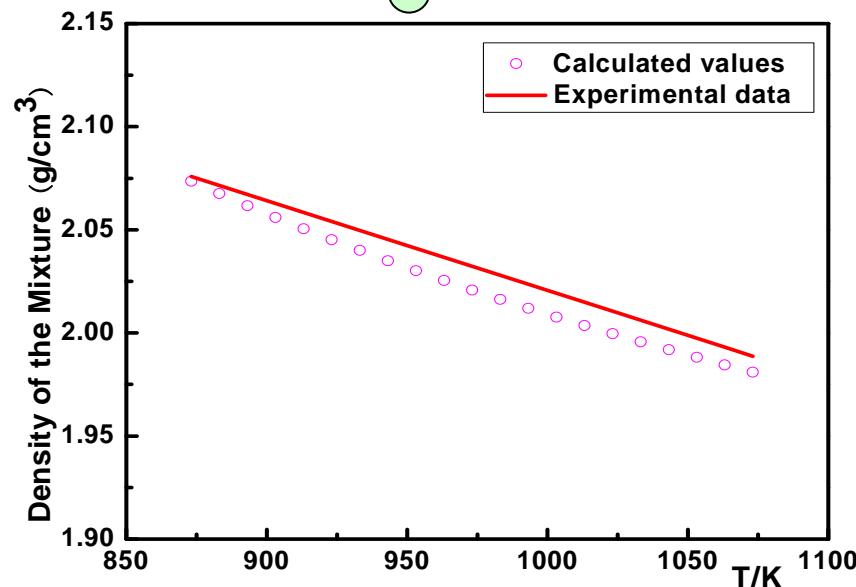




- Fundamental Research on MSRs
- Evaluation of static thermophysical properties

P-R Equation

$$p = \frac{RT}{v-b} - \frac{d}{v(v+b) + b(v-b)}$$



● 15LiF-58NaF-27BeF<sub>2</sub> in MOSART



### ➤ Fundamental Research on MSRs

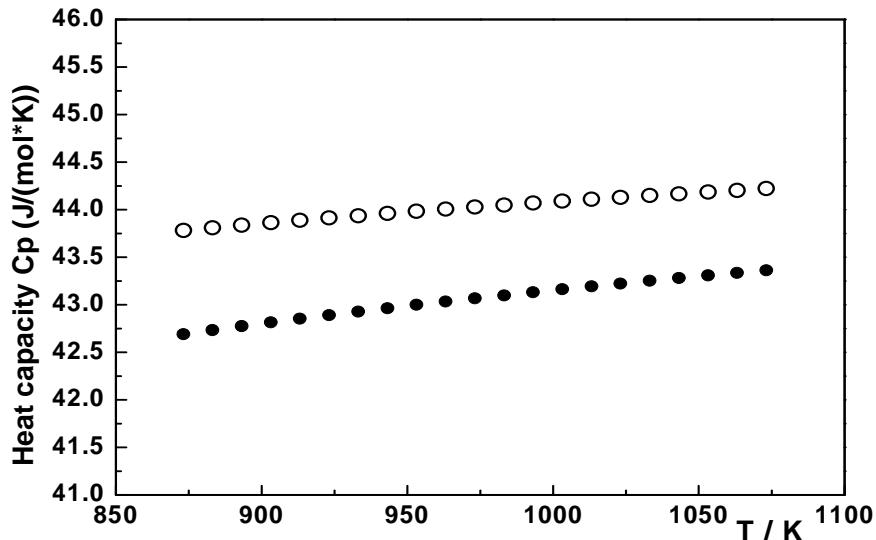
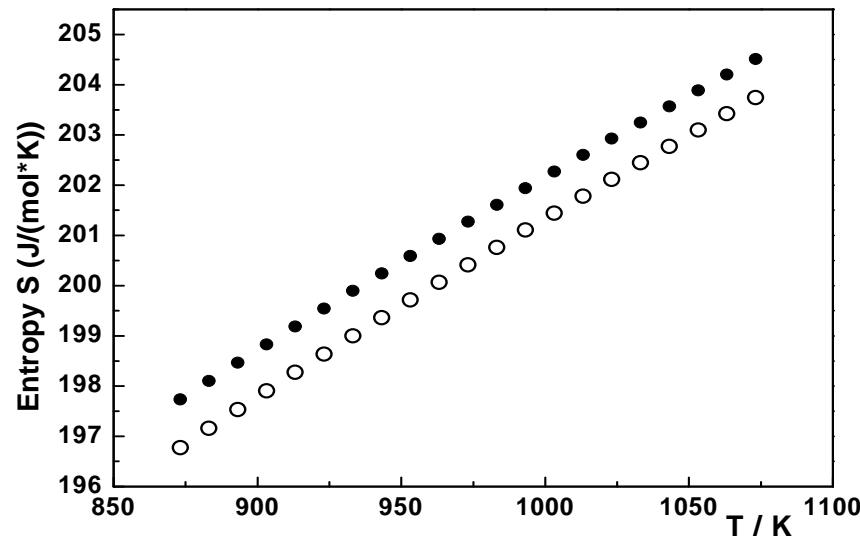
#### ● Evaluation of static thermophysical properties

✓ Residual function method

$$M_r = M_{p,t}^* - M_{p,t}$$

✓ Fugacity coefficient method

$$d\overline{G}_i = RTd(\ln \widehat{f}_i)_T$$



● 15LiF-58NaF-27BeF<sub>2</sub> in MOSART



- Fundamental Research on MSRs
- Neutron physics analysis
- Energy-time-space dependent neutronics model

## Equation for neutron flux:

$$\frac{1}{v(E)} \frac{\partial \phi(r, E, t)}{\partial t} = S(r, E, t) + \chi_p(E) \int_{E'} (1 - \beta) v \Sigma_f(r, E') \cdot \phi(r, E', t) dE' \\ + \sum_{i=1}^I \chi_{d,i}(E) \lambda_i C_i(r, t) + \int_{E'} \Sigma_s(r, E' \rightarrow E) \phi(r, E', t) dE' \\ - \Sigma_t(r, E) \phi(r, E, t) + \nabla \cdot D(r, E) \nabla \phi(r, E, t) - \frac{1}{v(E)} \nabla \cdot [U \phi(r, E, t)]$$

## Balance equation for delayed neutron precursors:

$$\frac{\partial C_i(r, t)}{\partial t} = \beta_i \int_E v \Sigma_f(r, E) \cdot \phi(r, E, t) dE - \lambda_i C_i(r, t) - \nabla \cdot [U C_i(r, t)]$$

Energy integration

□ Multi-group diffusion model

Convective



## ➤ Fundamental Research on MSRs

## ● Neutron physics analysis

$$\frac{1}{v_g} \cdot \frac{\partial \phi_g}{\partial t} + \boxed{\frac{1}{v_g} \nabla(U\phi_g)} = \nabla \cdot D_g \nabla \phi_g + \sum_{g'=1}^{g-1} \phi_{g'} \cdot \Sigma_{g' \rightarrow g} - \phi_g \cdot \Sigma_{r,g}$$

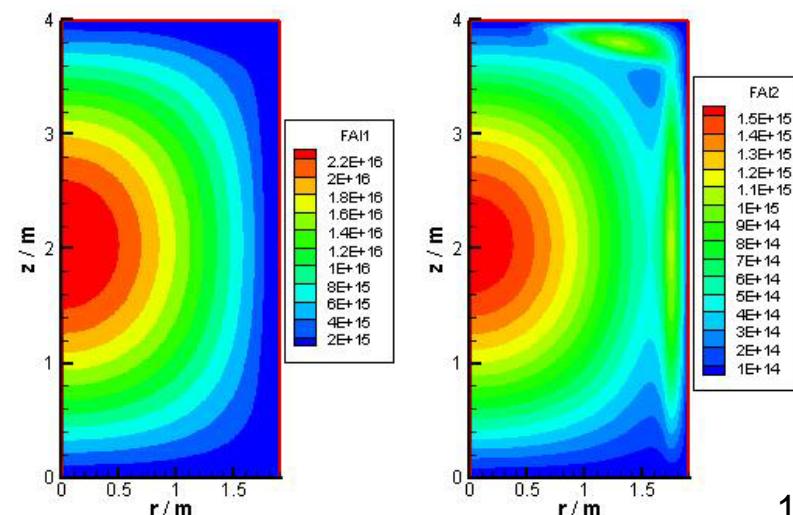
**Convective**  
 $+ \chi_{p,g} \cdot (1 - \sum_{i=1}^I \beta_i) \cdot \sum_{g=1}^G (\nu \Sigma_f)_g \cdot \phi_g + \sum_{i=1}^I \chi_{d,g,i} \cdot \lambda_i \cdot C_i$

$$\frac{\partial C_i}{\partial t} + \boxed{\nabla(UC_i)} = \beta_i \cdot \sum_{g=1}^G (\nu \Sigma_f)_g \cdot \phi_g - \lambda_i \cdot C_i$$

## ● For MOSART

Institute	Codes	$k_{\text{eff}}$
BME	MCNP4C + JEFF3.1	1.00905
FZK	2D560gr. + JEFF3.0	0.99285
NRG	MCNP4C + JEFF3.1	1.00887
Polito	2D4 gr. + JEFF3.1	0.99595
RRC-KI	MCNP4B+ENDF5,6	0.99791
SCK-CEN	MCNPX250	1.00904
XJTU	NPAC-XJTU	0.99994

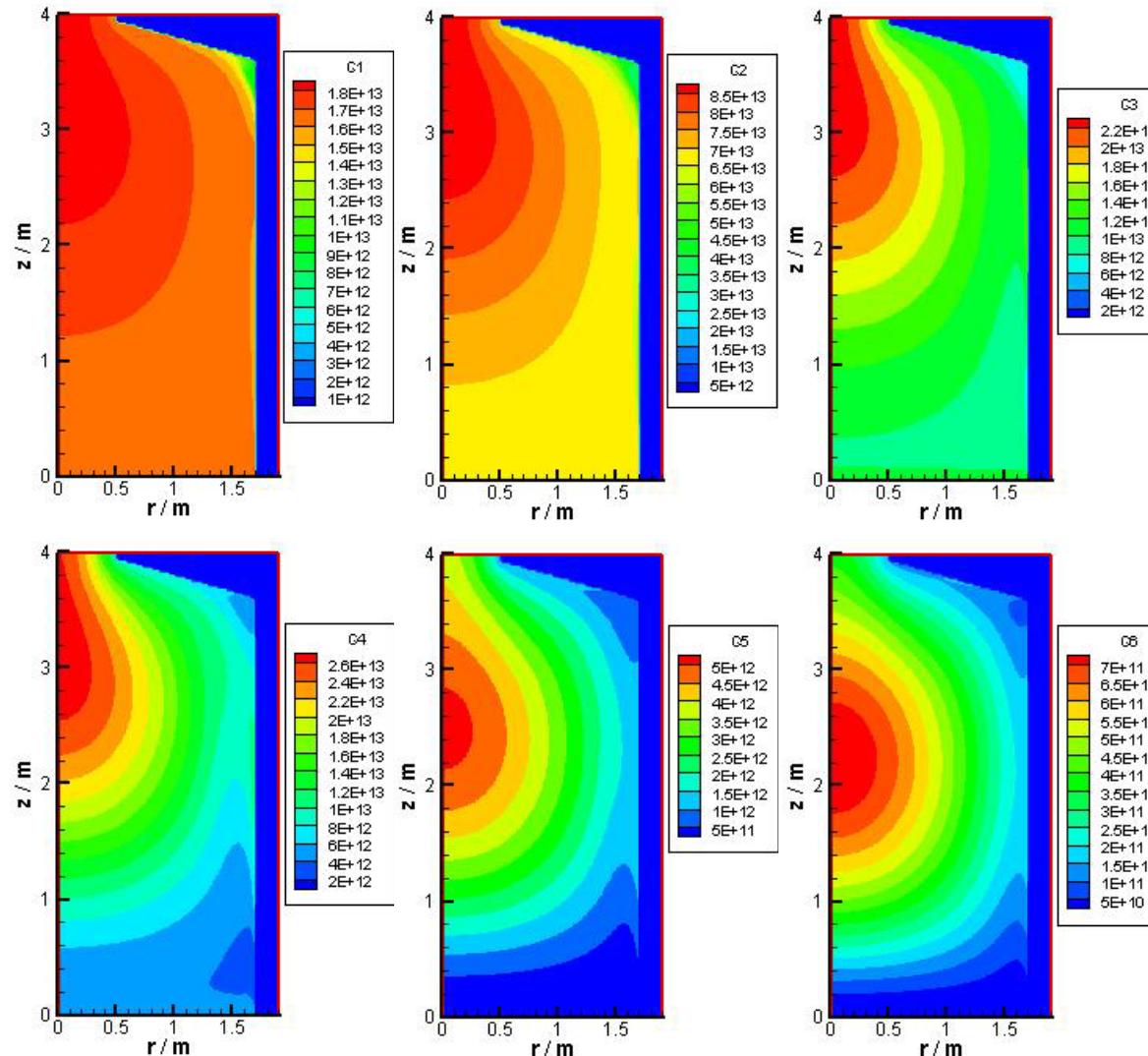
## □ Neutron fluxes





- Fundamental Research on MSRs
- Delayed neutron precursors

### ● Neutron physics analysis



### DNPs distribution show

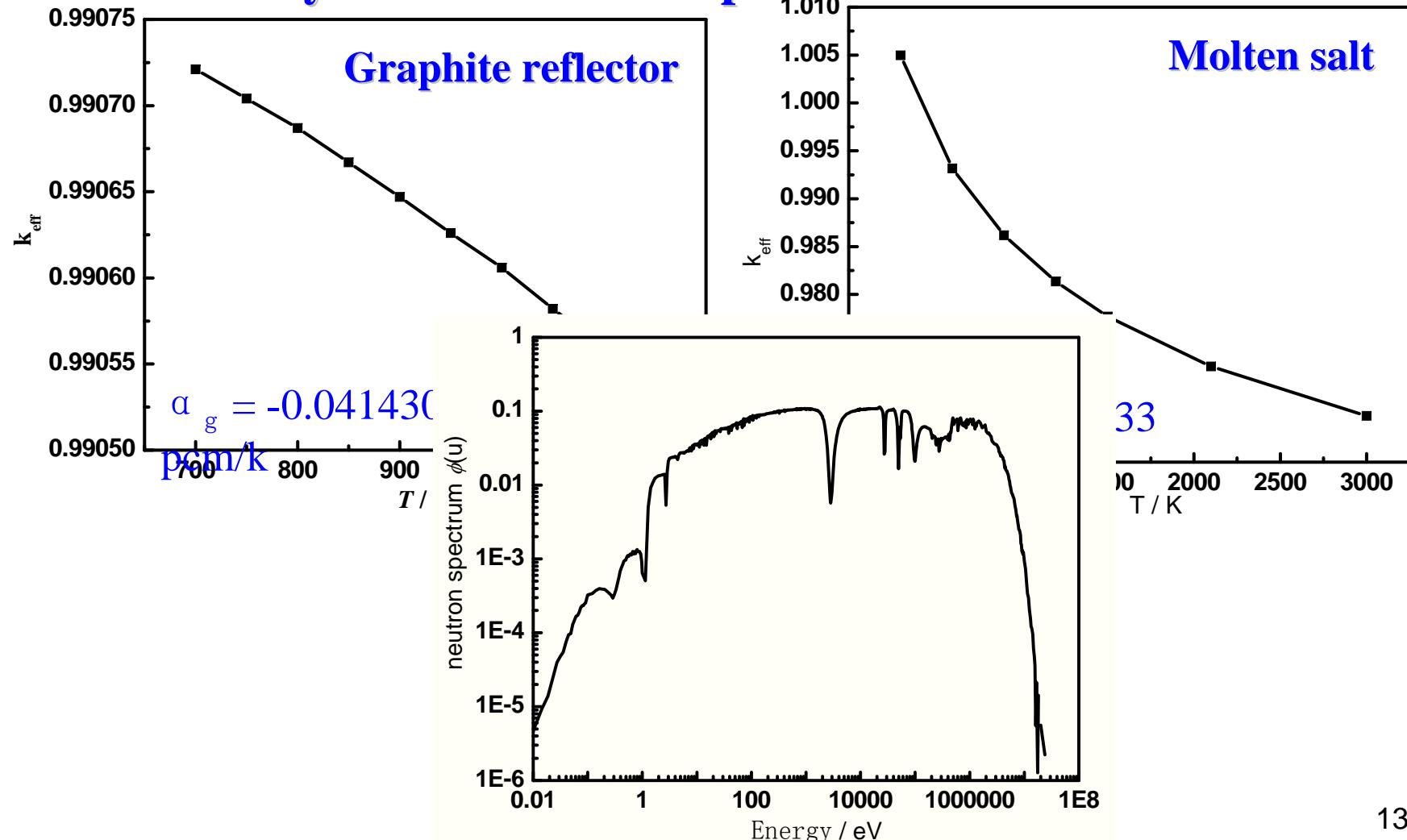
- ❖ Drift downstream with the flow;
- ❖ The larger the decay constant, the greater the flow effects.



### ➤ Fundamental Research on MSRs

### ● Neutron physics analysis

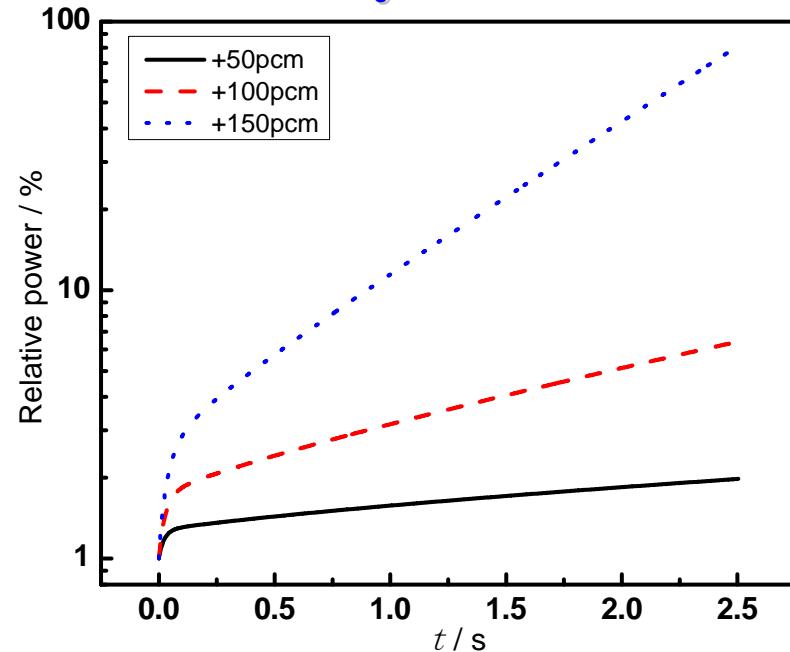
#### □ Reactivity coefficient of temperature





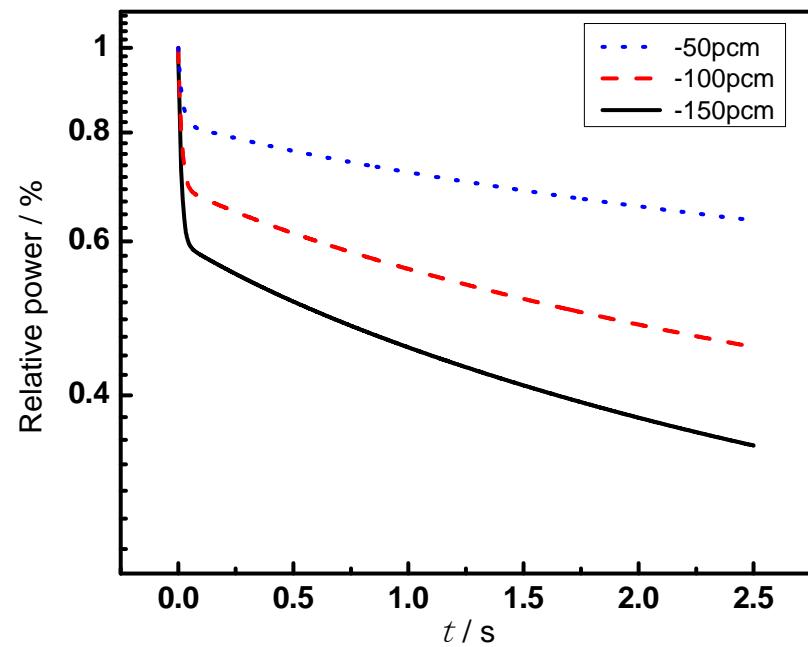
### ➤ Fundamental Research on MSRs

#### Reactivity increase



#### Neutron physics analysis

#### Reactivity decrease



The relative power increases (decreases) greatly in short time at beginning, then changes with a certain speed.

The larger the reactivity changes, the greater the initial power generates and the faster the changing speed is.



## ➤ Fundamental Research on MSRs • Thermal hydraulic analysis

- ✓ ORNL: there was no decisive difference between water and molten fluorides from the flow and heat transfer viewpoint .

### ➡ □ Computational Fluid Dynamic (CFD) method

$$\frac{\partial \rho u_z}{\partial z} + \frac{1}{r} \frac{\partial r \rho u_r}{\partial r} = 0$$

$$\frac{\partial(\rho u_z \cdot u_z)}{\partial z} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u_r \cdot u_z) = \frac{\partial}{\partial z} ((\eta + \eta_t) \frac{\partial u_z}{\partial z}) + \frac{1}{r} \frac{\partial}{\partial r} ((\eta + \eta_t) r \frac{\partial u_z}{\partial r}) + S_{u_z}$$

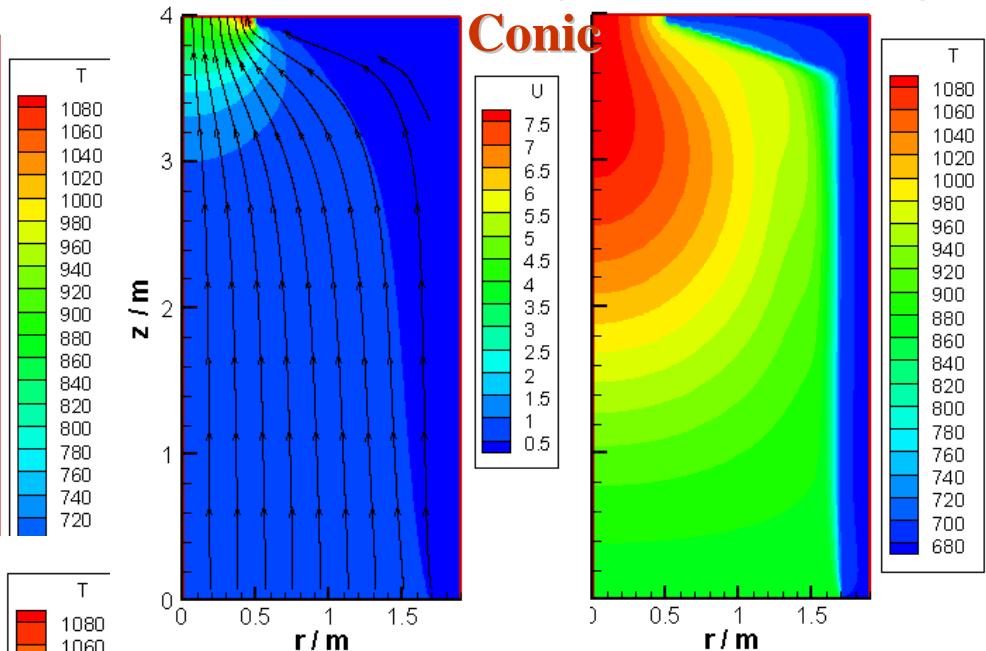
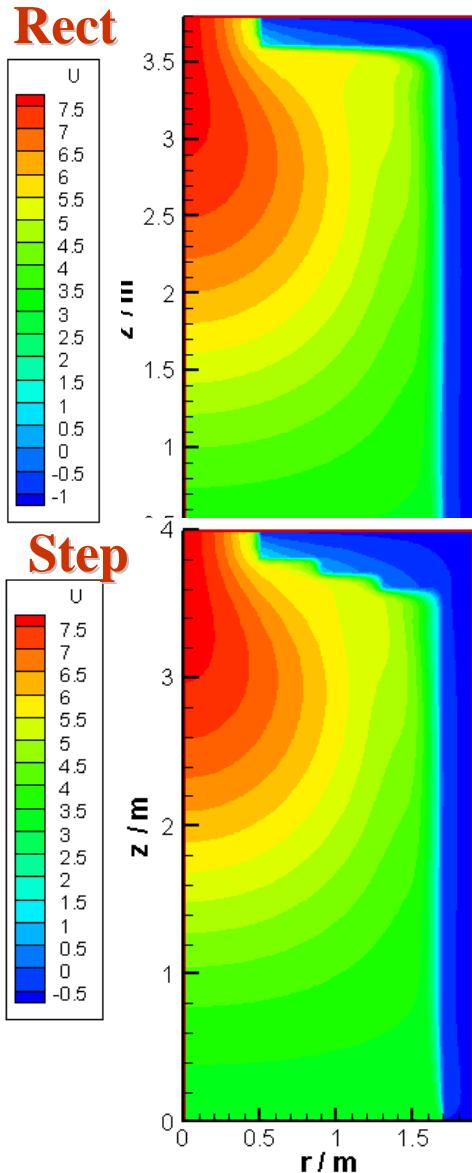
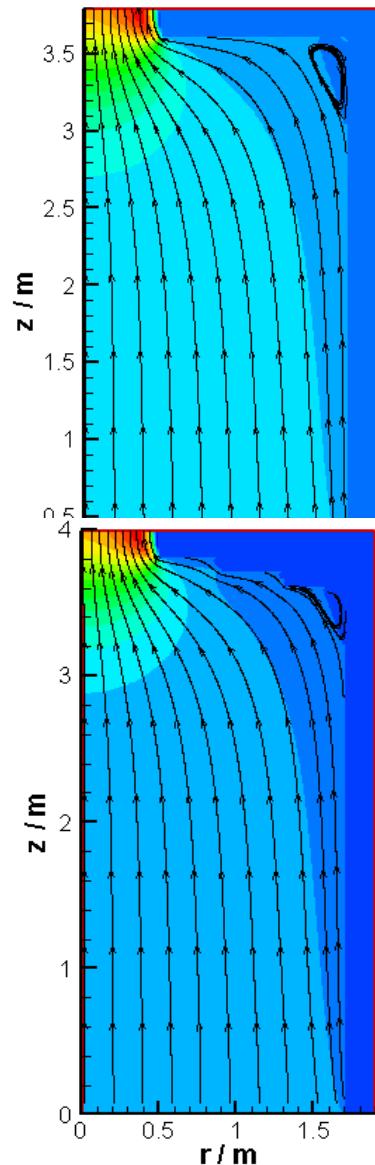
$$\frac{\partial(\rho u_z \cdot u_r)}{\partial z} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u_r \cdot u_r) = \frac{\partial}{\partial z} ((\eta + \eta_t) \frac{\partial u_r}{\partial z}) + \frac{1}{r} \frac{\partial}{\partial r} ((\eta + \eta_t) r \frac{\partial u_r}{\partial r}) + S_{u_r}$$

$$\frac{\partial(\rho u_z \cdot k)}{\partial z} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u_r \cdot k) = \frac{\partial}{\partial z} ((\eta + \frac{\eta_t}{\sigma_k}) \frac{\partial k}{\partial z}) + \frac{1}{r} \frac{\partial}{\partial r} ((\eta + \frac{\eta_t}{\sigma_k}) r \frac{\partial k}{\partial r}) + S_k$$

$$\frac{\partial(\rho u_z \cdot \varepsilon)}{\partial z} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u_r \cdot \varepsilon) = \frac{\partial}{\partial z} ((\eta + \frac{\eta_t}{\sigma_\varepsilon}) \frac{\partial \varepsilon}{\partial z}) + \frac{1}{r} \frac{\partial}{\partial r} ((\eta + \frac{\eta_t}{\sigma_\varepsilon}) r \frac{\partial \varepsilon}{\partial r}) + S_\varepsilon$$



### ➤ Fundamental Research on MSRs



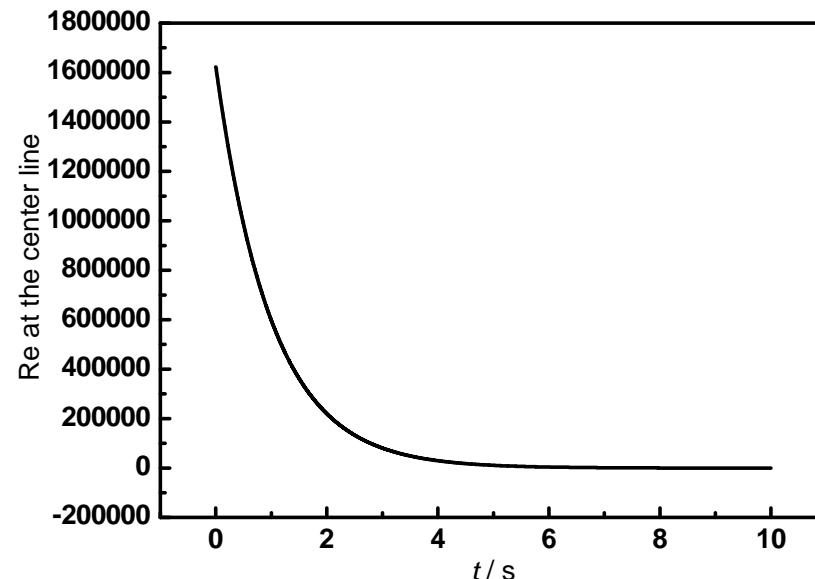
- Conic design satisfy:
  - Avoid reverse or stagnant flow
  - Maximum temperature is low enough



➤ Fundamental Research on MSRs  
● Thermal hydraulic analysis

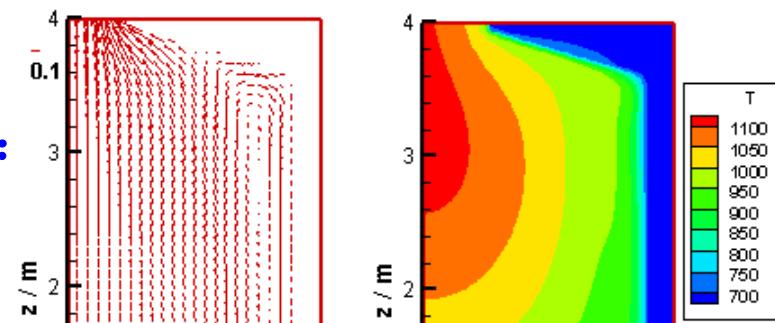
Flow decreases:

$$u_{in}(t) = u_{in}(0)e^{-\tau_{pump} \cdot t}$$

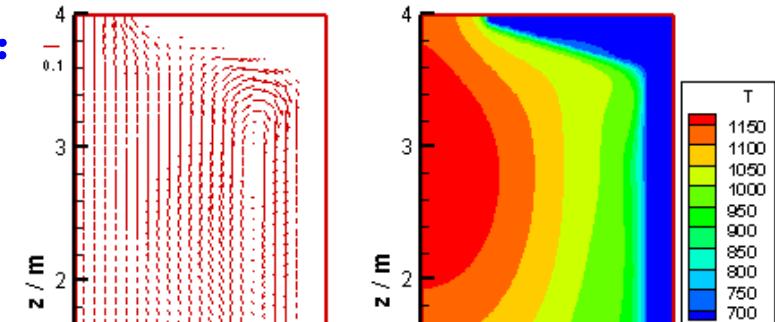


Re decreases exponentially,  
similar with the inlet velocity.

t=2s:

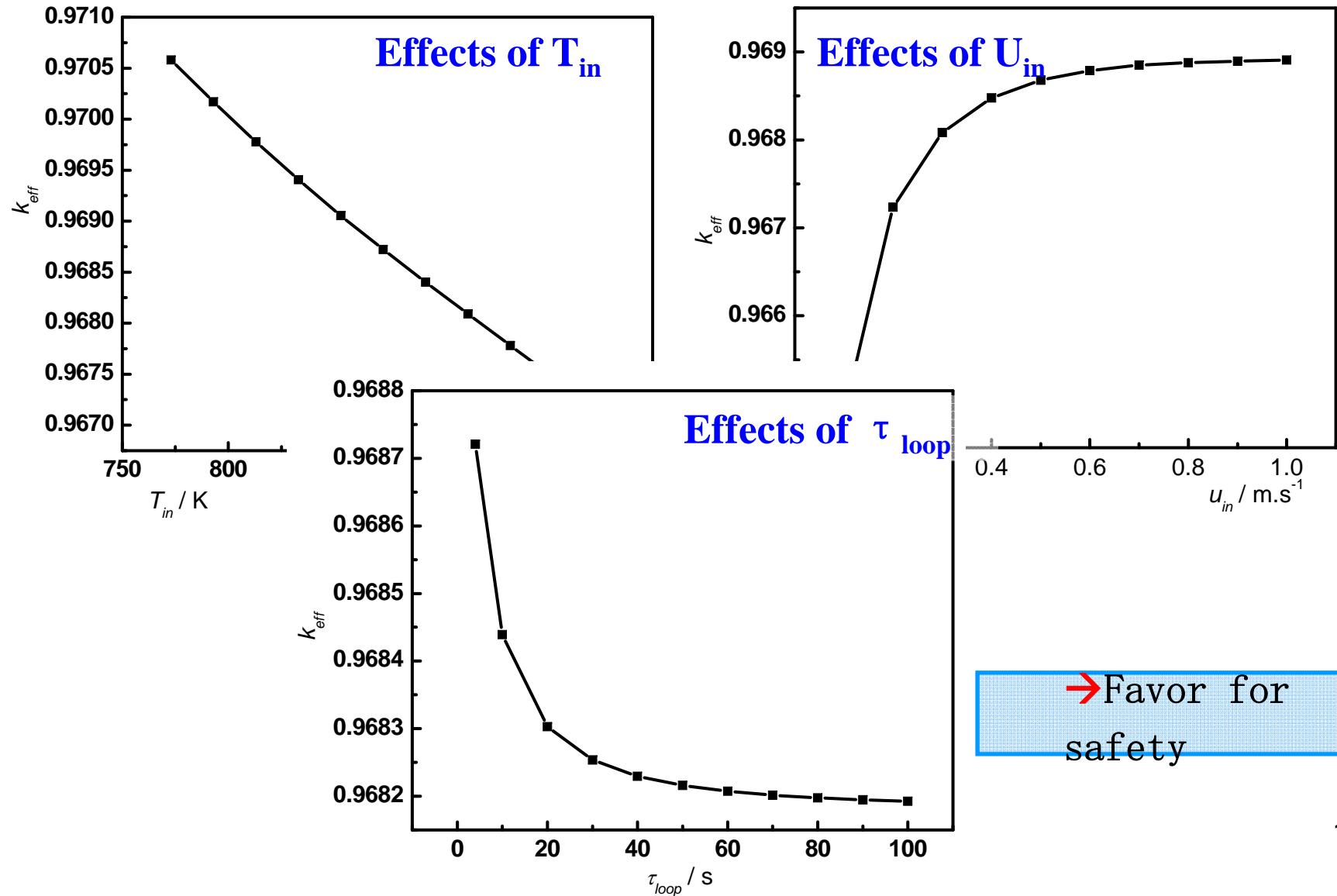


t=4s:





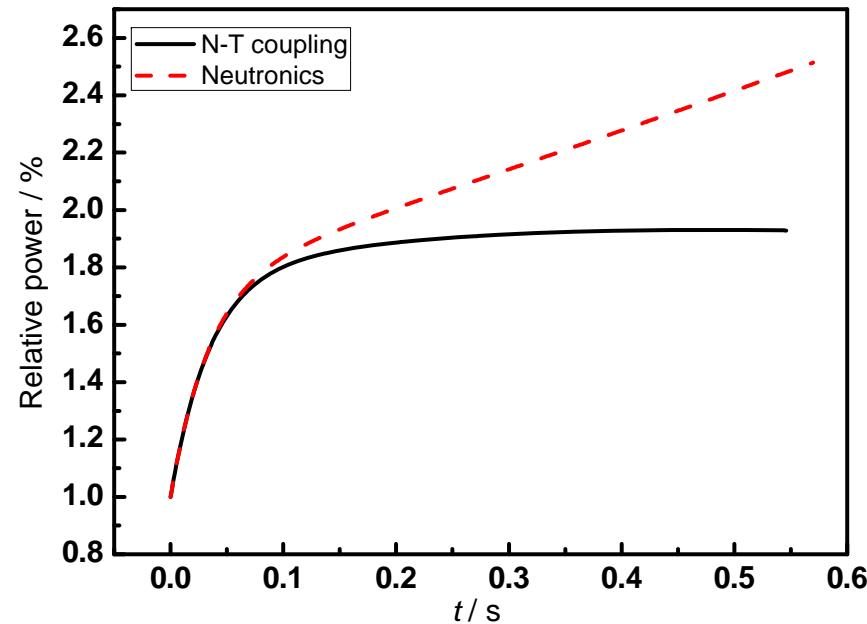
### ➤ Fundamental Research on MSRs ● N-T coupling: steady





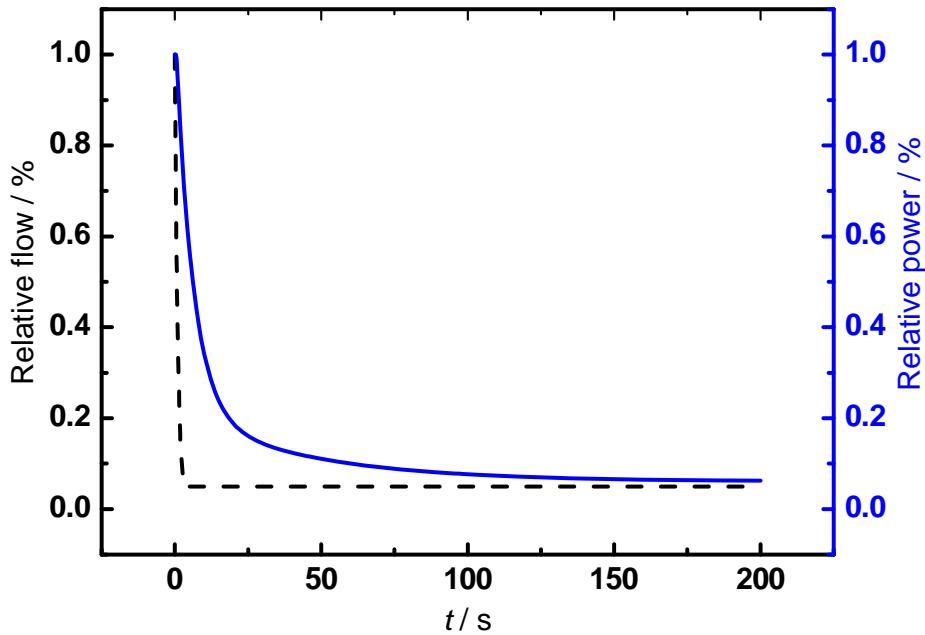
### ➤ Fundamental Research on MSRs ● N-T coupling: transient

□ Reactivity increases 100pcm:



Power increases suddenly, then slowly reaches a steady power.

□ Flow mass decreases:



Power decreases quickly with the flow, and slowly reaches the power matching with the flow



➤ **Fundamental Research on MSRs**      ● **Safety analysis**

□ **Exact point kinetic model:**

Based on the energy-time-space dependent neutronics model, using **perturbation theory**

$$\frac{dp_r(t)}{dt} = \frac{\rho(t) - \tilde{\beta}(t)}{\Lambda(t)} p_r(t) + \sum_{i=1} \lambda_i c_i(t)$$

$$\frac{d}{dt} c_i(t) = -\lambda_i c_i(t) + \frac{\tilde{\beta}_i}{\Lambda(t)} p_r(t) - \frac{(W, \chi_{di}(E) \nabla \cdot [\vec{U} C_i(r, t)])}{K_0}$$

$$\frac{\partial C_i(r, t)}{\partial t} + \nabla \cdot [\mathbf{U} C_i(r, t)] = -\lambda_i C_i(r, t) + \beta_i \mathbf{F} \phi(r, E, t)$$

where:  $\tilde{\beta}_i = \frac{(W, \chi_{di}(E) \lambda_i C_i(r, t))}{Y}$       (Effective fraction of DNPs)

**$W$  : Weighted function**



- **Fundamental Research on MSRs**
- **Neutron physics analysis**
- ✓ **Effective fraction of delayed neutron**
  - only considering the neutron importance disregarding the importance of delayed neutron

$$\nabla \cdot D_g \nabla \phi_g^* + \sum_{n=1, n \neq g}^G \Sigma_{g \rightarrow n} \phi_n^* - \Sigma_{r,g} \phi_g^* + (1-\beta)(v \Sigma_f)_g \sum_{n=1}^G \chi_{p,n} \phi_n^* = 0$$

$$\tilde{\beta}_i = \frac{(\phi^*, \beta_i \chi_{di}(E) F \phi)}{(\phi^*, \chi(E) F \phi)}$$

- **For MOSART**

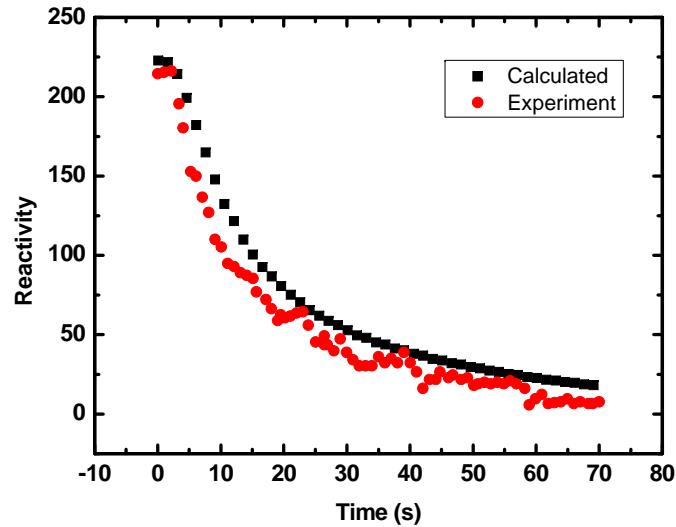
Velocity	$\Delta \rho$ [pcm]	$\beta_1$ [pcm]	$\beta_2$ [pcm]	$\beta_3$ [pcm]	$\beta_4$ [pcm]	$\beta_5$ [pcm]	$\beta_6$ [pcm]	$\beta_{eff}$ [pcm]	$\beta_{loss}$ [pcm]	$\beta_{loss} / \beta_{eff, static}$
Static	0.0	7.8	77.2	54.9	118.1	61.0	20.8	339.8	0.0	0.0 %
Flat	-115.2	3.7	37.3	28.9	78.4	56.4	20.5	225.2	114.6	33.7%
Parabolic	-131.8	3.6	36.4	27.1	69.3	53.0	20.1	209.5	130.3	38.4%
RRC-KI	-143.4	2.8	29.4	24.1	68.5	53.1	19.9	197.8	142.0	41.8%
XJTU	-127.0	3.6	36.3	27.5	70.5	53.5	20.1	211.5	128.3	37.8%



### ➤ Fundamental Research on MSRs

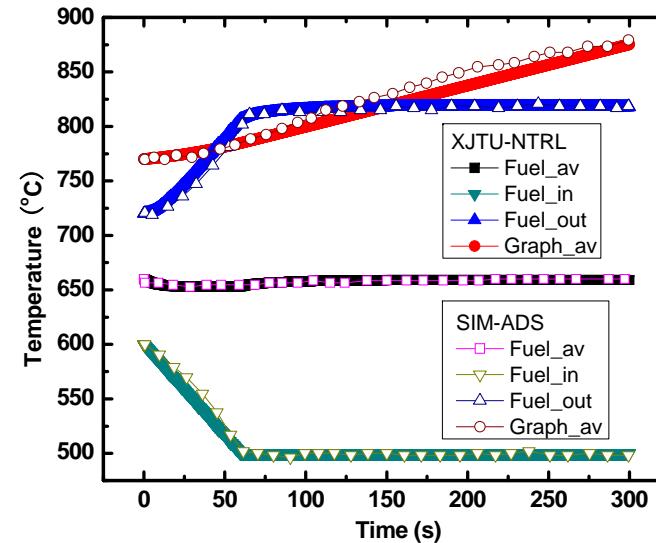
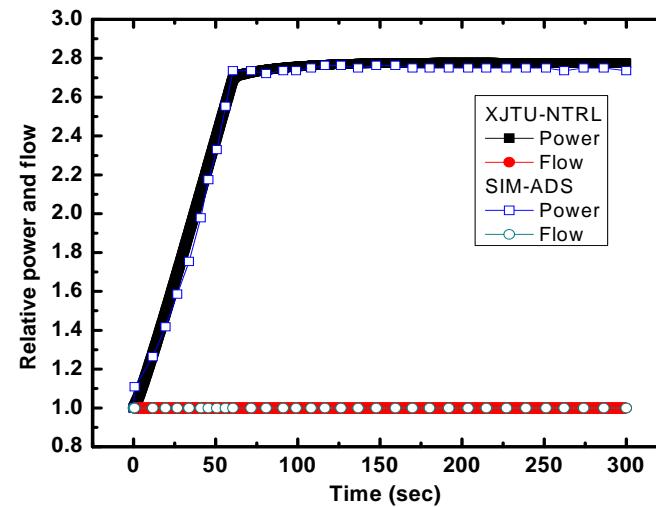
#### ✓ Modified point model ( $W = 1$ )

$$\left\{ \begin{array}{l} \frac{dn(t)}{dt} = \frac{(\rho(t) - \tilde{\beta}_{eff})}{\Lambda} n(t) + \sum_{i=1}^6 \lambda_i c_{c,i} \\ \frac{dc_{c,i}}{dt} = \frac{\beta_i}{\Lambda} n(t) - \lambda_i c_{c,i} + c_{l,i} \frac{1}{\tau_l} \left( \frac{V_l}{V_c} \right) - c_{c,i} \frac{1}{\tau_c} \\ \frac{dc_{l,i}}{dt} = -\lambda_i c_{l,i} + c_{c,i} \frac{1}{\tau_c} \left( \frac{V_c}{V_l} \right) - c_{l,i} \frac{1}{\tau_l} \end{array} \right.$$



↑MSRE:coastdown  
↓MOSART: UOC

#### ● Safety analysis





- Fundamental Research on MSRs
- ✓ Comparison of modeling options for delayed neutron precursor movement in molten salt reactors

$$\left. \begin{array}{l} \frac{dc_i(t)}{dt} = -\lambda_i c_i(t) + \frac{\beta_i}{\Lambda(t)} n(t) \\ \\ \frac{\partial C_i(r,t)}{\partial t} - \frac{(W, \chi_{di}(E) \nabla \cdot [\vec{U} C_i(r,t)])}{\partial C_i(r,t)} \\ + \nabla \cdot [\vec{U} C_i(r,t)] \frac{K^0}{F \phi n(t)} = -\lambda_i C_i(r,t) \end{array} \right\}$$

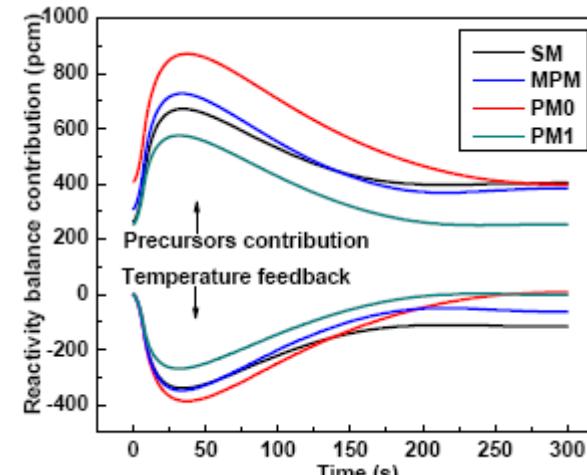
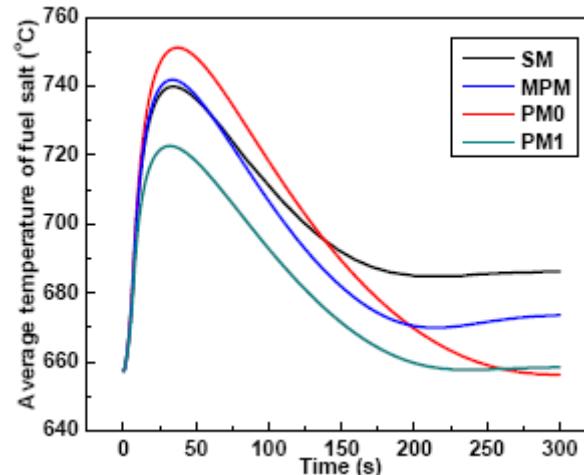
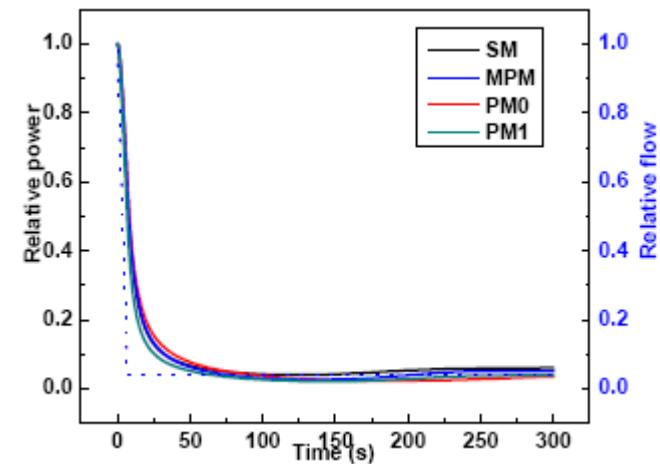
SM: spatial model

MPM: modified point model

PM: point model

- Safety analysis

- MOSART: ULOF





## ➤ Conclusion Remarks

- We studied the static thermophysical properties, neutron physics, thermal hydraulics, N-T coupling and safety characteristics by founding theoretical models and designing micro-computer codes.
  
- The established models are applied to MOSART, the results of which demonstrate the validation of the models.
  
- MOSART is a promising reactor with inherent safety ( negative temperature coefficient, flow effects...).



***Xi'an Jiaotong University***



***Nuclear Thermo-hydraulic  
Research Laboratory***

